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**Yuriy A. Drozd\*** (drozd@imath.kiev.ua), Tereshchenkivska str. 3, Kiev. *Representations of linear groups over Euclidean algebras*. Preliminary report.

We consider unitary representations of linear groups over algebras, i.e. groups  $GL(P, A) = \text{Aut}_A P$ , where  $A$  is a finite dimensional  $\mathbb{C}$ -algebra and  $P$  is a finitely generated projective  $A$ -module. We call the algebra  $A$  Dynkin (Euclidean) if it is derived equivalent to a path algebra of a Dynkin (respectively, Euclidean) quiver. In Dynkin case the author proved that the space  $\widehat{G}$  of unitary representations of such a group  $G$  contains an open dense subset  $U$  isomorphic to  $\widehat{GL}(r, \mathbb{C})$  for some  $r$ . For Euclidean algebras the following conjecture is plausible.

*If  $G$  is a linear group over an Euclidean algebra, then  $\widehat{G}$  contains an open dense subset  $U$ , such that  $U \simeq Q_m \times (\mathbb{C}^*)^k \times \widehat{GL}(r, \mathbb{C})$  for some  $m, k, r$ . Here  $Q_m = W_m/\mathbf{S}_m$ , where  $W_m = \{(\lambda_1, \lambda_2, \dots, \lambda_m) | \lambda_i \in \mathbb{C}, \lambda_i \neq \lambda_j \text{ for } i \neq j\}$  and  $\mathbf{S}_m$  is the symmetric group naturally acting on  $Q_m$ .*

This conjecture was proved by Timoshin for  $A$  of type  $\widetilde{A}_1, 2$ . We present a proof for  $A$  of type  $\widetilde{A}_n$ . This proof is based on the technique of matrix problems, especially on the algorithm of small reduction. (Received February 01, 2008)